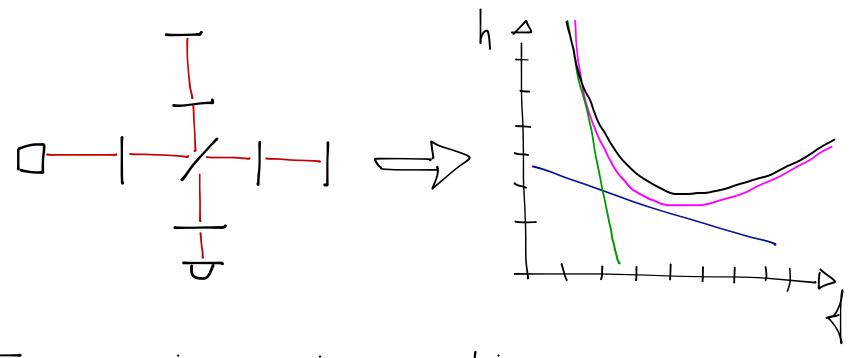
SIGNALS + NOISE



This session: Signals + Norse
What is a signal?
What is norse?
How to compute a signal response?
How to use the frequency domain?
How to compute a sensitivity curve?

Signal and 'noise' are not well defined, there meaning chays with context.
One preson's signal is another one's noise!

Possible mathematical definition
Norse output from a random (stochastic) process
Signal output from a coherent process

Possible project defention Noise unwanted output

Signal: Wanted output

Can junthink af examples where these definitions are compatible or not compatible?

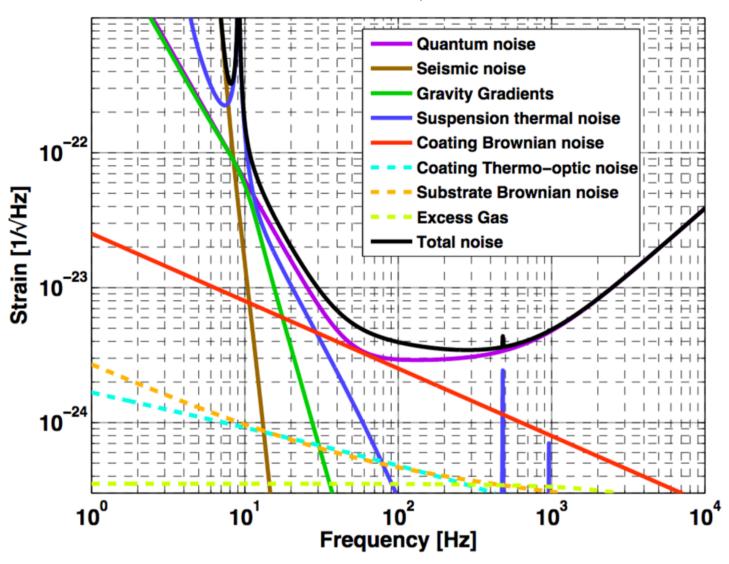
Signal and Noise in LIGO

In operation output from any known of gravitational wave is a signal Everything else is morse GWs can be coherent (CW, inspiral) or stochashic (burst, background)

During commissioning we do not look for GWs Instead we perform
experiments to Industrial the Gehaviour of the instrument
Then Synchs are typically created on purpose, such as
coherent mirar motion, coherent modulation of the last
frequency, etc

Projected (modelley) sensitivity to guide the instrument design

what are these?





In Certain conditions we can describe n(t) by its frequency Components, also called in the frequency domain!

This is true for time invariant processes in linear systems Simple and weful because:

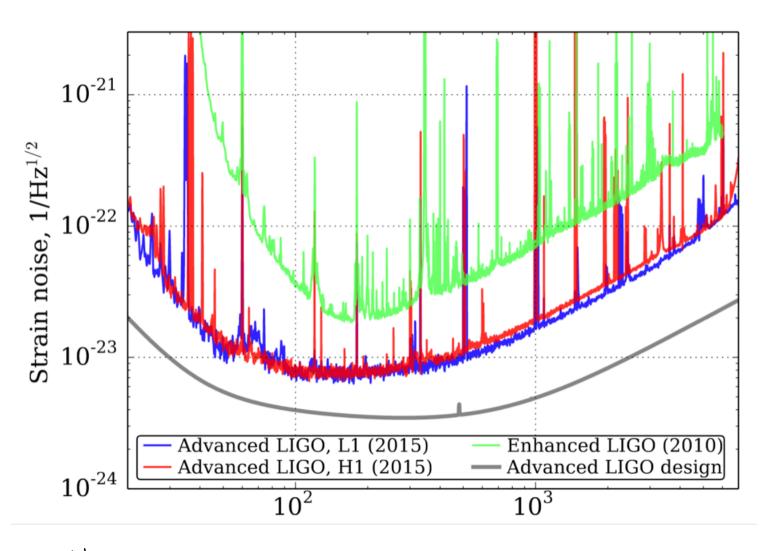
- frequency components do not mix, can be computed separately Components can be added (superposition principle)

LIGO is not always that simple, but approaches that state in Science mode

Generally useful to understand the simpler frequency domain version of a system if possible

99% of all 460 modelling in the frequency domain

Measured sensitivity to compare performances



How to generate such plots?

Some basic features of the plot. x-axis of the Fourth frequency of a signal or noise component [Hz] y-axis h, garitational wave strain, with h = DL/L with units Hz, it is an Amplitude Spectral Density (ASD) Very Srief introduction into spectral densities Lets start with a random process (stationary, i.e. time invarient) n(t) P

L5

How to get a description of 'n' in the frequency domain? With the Towier transform:

$$m(1) = FT(n(t)) = \int_{-\infty}^{\infty} n(t) e^{-i2\pi t} dt$$

We measure for a limited time T and only get:

$$m_{T}(1) = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} n(t) e^{-i2\pi i t} dt$$

Most sandom processes have average constant power so that MT(y) v T, ie different results for different measurement times. Instead a more useful spetral representation is the power spectral density:

Power Spetral Density (PSD) Sn (1)= lim = | St (n(t)-n)e-12 t of | 2 mean of n(t)

Amplitude Spectral Density (ASD) (Sn(1), used because has often intulite units In practise: - measure n(t) over T - Thmore mean \(\frac{1}{n} \) Depends on FFT Junction! - Compute FFT - Square, (multiply by =) 29 vare 200t

Units of moise curres

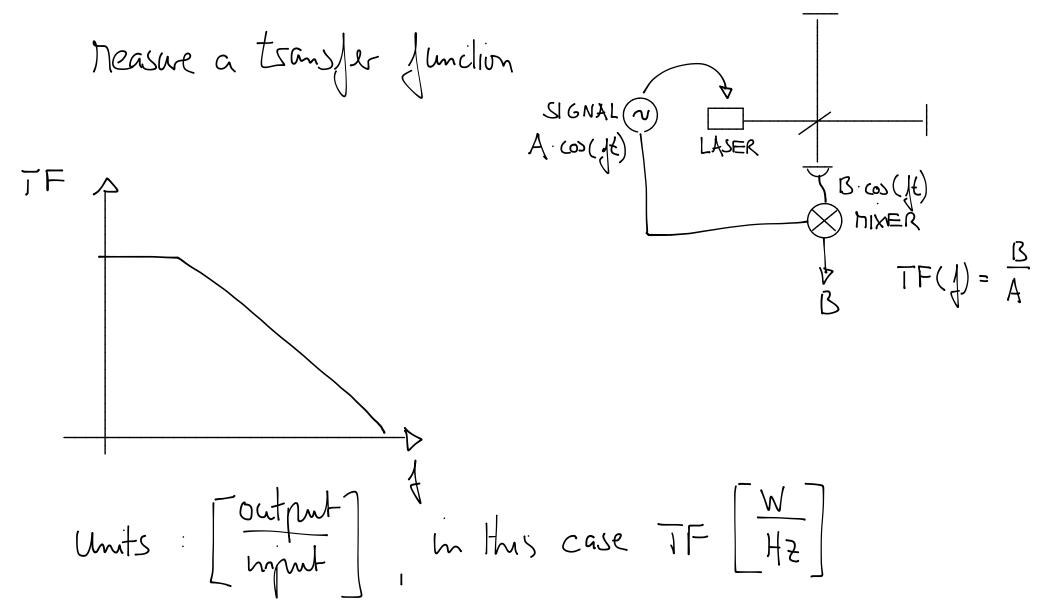
Example n(t) [m]

m(1) [m s] = $\left[\frac{m}{Hz}\right]$ Fower transform

 $S_m(1)$ $\left[\frac{m^2}{Hz^2} \cdot S\right] = \left[\frac{m^2}{Hz}\right]$ power spectral density

(Sn(1) [m] amplitude spetral density

LIGO Design example: Want to compare last frequency noise to a minor motion noise. ASD HZ Howt compare? ASOM [HZ] Idea | can compare the noise each would generate in the output ASDOW HZ ON IN FINESSE [W] Need to Jud a way to compute output spetom from uput spectorm & need Fransle Function ASDout(1) = ASDin (1). TF (1) Junction of the inter-ferometer LJ

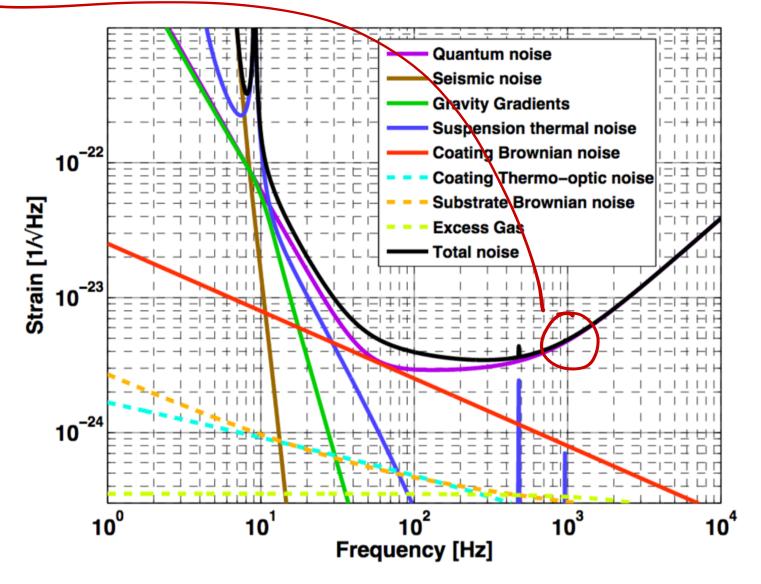


/12

Reape for sensitivity plat For each move -obtain input spetrum (measure, or theoretical prediction)
- compute transfer function to out put TFN [Noise] - computer transfer Junction for GW signal to out put - Compute norse in units of h as $n(y) \cdot \frac{TF_{GW}}{TF_{GW}}$ - add cure to plot - add curre to plot

Sum (squared) all curves for 'total moisi'

At 1000 Hz, the morse (quantum) has a maynitude comparable to a GW signal of 5 10-24 Hz Note easy to compare morse to morse



/14

L5

Summary

- for moise we use ASD to grantify + compare
- We we signal TFs to project noise from one point in the system to other
- Sensitivity plot are move curves projected to GW signal